INTRODUCING EQUIBEL

AN IMPLEMENTATION OF CONSISTENCY-BASED BELIEF CHANGE

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- We have a network of agents
- Each agent has some initial beliefs about the state of the world
- Agents communicate and share information
- **Goal:** Determine what each agent believes after learning as much as possible from other agents
- **How do we do this?**

Original Graph $G$

Completion of $G$
Example: Drones looking for people in a disaster site

- Each drone has an initial belief:
  - Drone 1 believes that there is a person in the bookstore, and one in the atrium: $b \land a$
  - Drone 2 believes that there cannot be missing people in both the atrium and the bookstore: $\neg b \lor \neg a$
  - Drone 3 just believes that there is a person in the cafeteria: $c$

- The drones communicate, and learn from one another
  - Each drone is willing to incorporate new information that does not conflict with its initial beliefs
An agent starts out with initial beliefs that it does not want to give up, and then includes as much information as consistently possible from other agents.

We want to determine what *pieces of information* an agent can incorporate from others.

**How is this done?**

- Agent $i$ expresses its beliefs in a language $\mathcal{L}^i$ over superscripted atoms $\mathcal{P}^i = \{p^i, q^i, r^i, \ldots\}$ (i.e. agent 1 believes $p^1 \land \neg q^1$)
- We “force” the *languages* used by adjacent agents to agree on the truth values of corresponding atoms *as much as consistently possible*
- This yields one or more maximal sets of equivalences, $EQ$, between atoms in the languages of adjacent agents.
- These equivalences provide a means to *consistently translate* information from one agent to another.
**Purpose:** To make it easy for students and researchers to experiment with belief change

- Equibel is an implementation of the consistency-based framework, in ASP and Python
- Allows users to *simulate* belief sharing in arbitrary networks of agents
  - Users create a graph and assign formulas to nodes
- Supports standard belief change operations like revision and merging by automatically constructing *implicit graph topologies*
  - Users specify a set of formulas and an operation to be performed
  - Behind the scenes, Equibel constructs a graph, finds the completion, and returns only the relevant formulas
The main operation performed by Equibel is finding the completion of a $G$-scenario.

The steps to find the completion are:
1. Find maximal sets of equivalences between atoms of adjacent agents
2. Translate beliefs between the languages of adjacent agents
3. Combine beliefs resulting from different maximal equivalence sets

Two architectural layers:
- The ASP layer performs the core maximization procedure
- The Python layer post-processes answer sets and provides programmatic and interactive interfaces
EQUIBEL SYSTEM DESIGN

Python

equibel Module / Interactive CLI

Classes for Graphs, Formulas, etc.

Format Converters

gingo Module

ASP

eq_base.lp

cardinality.lp

...  

containment.lp

Modular Logic Program Structure

input.bcf

output.bcf
- The graph structure is encoded using `node/1` and `edge/2`, and formulas are associated with nodes using `formula/2`.
- Formulas are created using `neg/1`, `and/2`, `or/2`, `implies/2`, and `iff/2`.

**Example**

```
node(1). node(2). node(3). node(4).
edge(1,2). edge(1,3). edge(2,3). edge(2,4).
formula(1, and(p,q)).
formula(2, or(q,neg(r))).
formula(3, implies(and(p,neg(q)),neg(r))).
formula(4, p).
```
First, we break down formulas into subformulas and extract atoms

- We generate candidate equivalences $p^x \equiv p^y$ with:

\[
\{ \text{eq}(P,X,Y) : \text{atom}(P), \text{edge}(X,Y), X < Y \}.
\]

- Then we attempt to assign truth values to the atoms at each node:

\[
1 \{ \text{tv}(N,P,1) ; \text{tv}(N,P,0) \} 1 : - \text{atom}(P), \text{node}(N).
\]

- Such that atoms $p^x$ and $p^y$ that participate in an equivalence $p^x \equiv p^y$ have the same truth value:

\[
: - \text{eq}(P,X,Y), \text{edge}(X,Y), \text{tv}(X,P,V), \text{tv}(Y,P,W), V \neq W.
\]

- We build up the original formulas from the bottom-up, checking satisfiability; all agents’ original formulas must be satisfied:

\[
: - \text{formula}(N,F), \text{not sat}(N,F).
\]
ASP gives us a collection of maximal equivalence sets

In Python, we translate formulas between the languages of connected agents based on the EQ sets

An agent may obtain different information from different EQ sets
  - Each EQ set represents an equally plausible way to share information
  - So we take the disjunction of beliefs obtained from different EQ sets

**Possible Propagation Scenarios**

**Input Scenario**
- $p$
- $p \land q$

1 2 3

**Completion**
- $p \land q$
- $q$
- $p \land q$

1 2 3

EQ = \{ $p^1 \equiv p^2$, $q^1 \equiv q^2$, $q^2 \equiv q^3$\}

EQ = \{ $p^2 \equiv p^3$, $q^1 \equiv q^2$, $q^2 \equiv q^3$\}
Equibel can be used interactively, by invoking the equibel prompt:

```plaintext
equibel (g) > add_nodes [1..4]
  nodes: [1, 2, 3, 4]
equibel (g) > add_edges [(1, 2), (2, 3), (3, 4)]
  edges: 1 <-> 2  2 <-> 3  3 <-> 4
equibel (g) > add_formula 1 p & q
  node 1: q & p
equibel (g) > add_formula 4 ~p & r
  node 4: ~p & r
equibel (g) > completion
  node 1: q & p & r
  node 2: q & r
  node 3: q & r
  node 4: q & ~p & r
```
The following script simulates belief sharing in the drone scenario:

```python
import equibel
G = equibel.complete_graph(3)
G.add_formula(0, 'a & b')
G.add_formula(1, '~a | ~b')
G.add_formula(2, 'c')
R = equibel.completion(G)
print(R.formulas())
```

```
{0: a & c & b, 1: c & ((a & ~b) | (~a & b)), 2: (a | b) & c}
```
**Belief revision** = Incorporating a new belief $\alpha$ into a belief set $K$

$\text{equibel.revise}([\{p', 'q | \sim r\}], 'r')$ constructs the graph:

Agent 2 will incorporate as much information as possible from agent 1, while not giving up its initial belief.

The *revision* of $K = \{p, q \lor \sim r\}$ by $\alpha = r$ is the belief of agent 2 in the completion.
Two types of merging: projection-based and consensus-based

```python
equibel.merge(['p&q', '~p|r', 'q->r'],
type=equibel.PROJECTION) constructs a star graph:
```

- The input formulas are *projected* onto the central node
- The result is the formula at the central node in the completion
Equibel

- Is a software system for working with equivalence-based belief change
- Simulates belief sharing in multi-agent scenarios
- Supports standard belief change operations (revision and merging) by constructing implicit graphs
- Provides a Python package, as well as an interactive prompt
- Is open source, hosted at www.github.com/asteroidhouse/equibel
- Is available on PyPI, so it can be installed using pip:

  ```
  pip install equibel
  ```